15-211: Assignment 4

Theory Questions

Due: June 13, 2008 in class

These questions count for 15% of the homework grade. Please hand in your answers in lecture on Friday.

1 Huffman vs. LZW (8 pts)

- (a) (2 points) Quantra Disk Company has come up with a hard drive that can store 4 possible values in each cell (0,1,2,3) rather than the typical (0,1). How can you modify the Huffman Encoding algorithm to take advantage of this new technology?
- (b) (2 points) You initialize your dictionary for LZW compression with 256 elements. Then, you read in 69 bytes from a file you want to compress. What is the minimum and maximum number of entries in the dictionary?

Minimum: 256 + _____

Maximum: 256 + _____

(c) (4 points) Suppose you're compressing a file consisting of a's,b's,c's, and d's with LZW. Your initial dictionary thus has only four elements (a=0, b=1, c=2, d=3). You want to compress the following string:

baadcaadaad

Show the end dictionary after you run LZW:

a=0	
b=1	
c=2	
d=3	

What does it compress to?

2 Burrows-Wheeler (7 pts)

(a) (1 point) Encode the following string of numbers using Huffman encoding: 01212312

What is the length of the result in bits?

(b) (2 points) Perform the Burrows-Wheeler transform on the original string: $01212312\,$

What is the resulting string?

(c) (2 points) Perform the Move-To-Front transform on your string from the previous part. The initial dictionary is as follows:

[0,1,2,3]

What is the resulting string?

(d) (2 points) Why does the Burrows-Wheeler transform followed by Move-To-Front generally result in smaller Huffman compressed files?