

Lecture 19: Allosteric Inhibitors

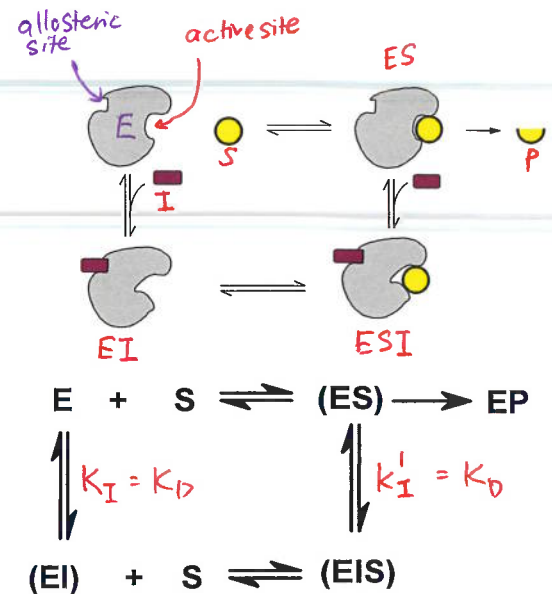
The binding site of the inhibitor is **not** at the active site. The inhibitor does not look like the substrate.

- The binding is reversible.
- The inhibitor can bind to both [E] and [ES].
- The inhibitor binding causes a change in the conformation of the protein that affects either substrate binding, the chemical step, or both.

There are two K_D values that describe the binding.

$$K_I = \frac{[E][I]}{[EI]} = K_D$$

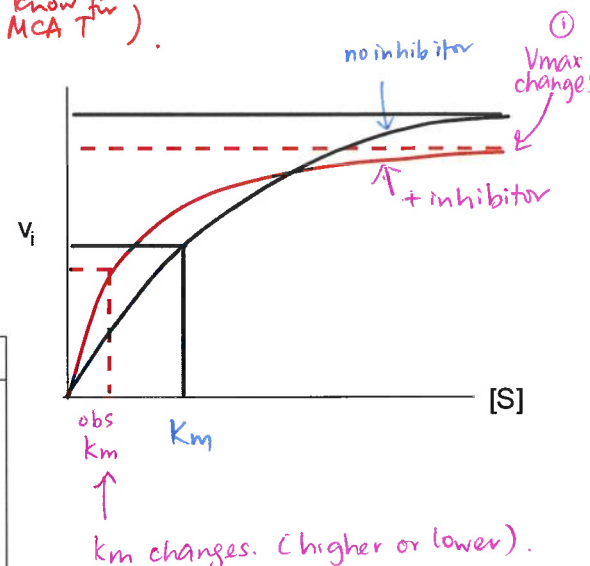
$$K_I' = \frac{[ES][I]}{[ESI]} = K_D$$



Special Cases of Mixed-type Inhibition:
(Unrealistic simplifications).

| | Binds to (E) | Binds to (ES) |
|-------------------|---------------|---------------|
| Mixed type | yes | yes |
| Uncompetitive | no | yes |
| Noncompetitive | Same affinity | Same affinity |

general case
special (MCA Tth) cases



- Both V_{MAX} and K_M can be altered by mixed inhibitors since the precise geometry of the active site is altered when the inhibitor is bound, potentially affecting binding and catalysis.
- The change in V_{MAX} and K_m can be used to find K_I and K_I' .

α = ratio of slopes
(+I/no inh)

$$K_I = [I]/(\alpha - 1)$$

α' = ratio of y-intercept
(+I/no inh)

$$K_I' = [I]/(\alpha' - 1)$$

No Inhibitor Present

$$v = V_{MAX} \frac{[S]}{K_M + [S]}$$

$$\frac{1}{v} = \frac{K_M}{V_{MAX}} \frac{1}{[S]} + \frac{1}{V_{MAX}}$$

slope

y intercept.

slope

y intercept.

change in slope gives α , as previously.

change in y-intercept give α'

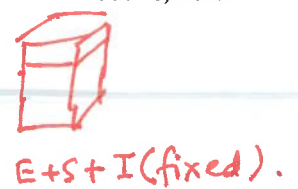
| Mixed Inhibitor |
|--|
| $\alpha = 1 + \frac{[I]}{K_I}$ |
| $\alpha' = 1 + \frac{[I]}{K_I'}$ |
| $v = \frac{V_{MAX}}{\alpha'} \frac{[S]}{\alpha K_M + [S]}$ |
| $\frac{1}{v} = \frac{\alpha K_M}{V_{MAX}} \frac{1}{[S]} + \frac{\alpha'}{V_{MAX}}$ |

can get K_I & K_I' from changes in K_m and V_{max}

Obtaining K_i and K_i' for Mixed Inhibitors:

A. Data Collection.

1. Obtain v versus $[S]$ in the *absence* of inhibitor.
2. Obtain v versus $[S]$ in the *presence* of a *fixed* and *known* concentration of inhibitor.



B1. Direct Fitting to Data:

1. Predicted velocities: $v_{pred} = \frac{v_{MAX}[S]}{\alpha K_M + [S]}$
2. Determine difference between observed and predicted:
 $\chi^2 = \sum (V_{obs} - V_{pred})^2$
3. Use Solver to find best fit to data by varying K_M , V_{MAX} , α , and α' .
4. $K_I = \frac{[I]}{(\alpha - 1)}$ and $K_I' = \frac{[I]}{(\alpha' - 1)}$

recitation.

B2. Double Reciprocal Plot:

1. Plot both data sets on a double reciprocal plot
2. α = ratio of the slopes.
3. α' = ratio of Y-intercepts.
4. $K_I = \frac{[I]}{(\alpha - 1)}$ and $K_I' = \frac{[I]}{(\alpha' - 1)}$

Example:

| [S] mM | v ([I]=0) | v ([I]=10 μ M) | $1/S$ | $1/V$ ([I]=0) | $1/V$ ([I]=10 μ M) |
|--------|----------------|-------------------------|-------|------------------|---------------------------|
| 1 | 16.7 | 2.9 | 1.0 | 0.060 | 0.340 |
| 5 | 50.0 | 10.0 | 0.2 | 0.020 | 0.100 |
| 10 | 66.7 | 14.3 | 0.1 | 0.015 | 0.070 |
| 20 | 80.0 | 18.2 | 0.05 | 0.0125 | 0.055 |

K_I - Obtain α - ratio of slopes.

Slope ([I]=0): 0.05 Slope ([I]>0): 0.3

$\alpha = \text{slope}([I]>0) / \text{slope}([I]=0) = 6$

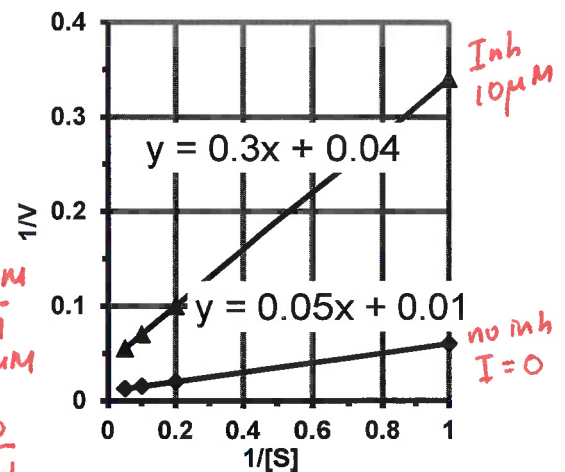
K_I' Obtain α' - ratio of y-intercepts:

0.01 \leftarrow y-int([I]=0): 0.01 y-int([I]>0): 0.04

$\alpha' = \text{y-int}([I]>0) / \text{y-int}([I]=0) = \frac{0.04}{0.01} = 4$

$K_I = \frac{10 \mu\text{M}}{6-1} = 2 \mu\text{M}$

$K_I' = \frac{10}{4-1} = 3.3 \mu\text{M}$



Use of double reciprocal plots to distinguish between inhibitor types.

- i) Draw a line representing the un-inhibited reaction, label the intersection with the y-axis.
- ii) Draw a line representing a competitive inhibitor. (V_{max} unchanged, K_M increased)
- iii) Draw a line representing an allosteric inhibitor (V_{max} & K_M change)

