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4	The Art of Wrangling: Working with Web-based Visual World Paradigm Eye-tracking
5	Data in Language Research
6	Authors: Adam A. Bramlett <sup>1</sup> , Seth Wiener <sup>2</sup>
7	Affiliation: <sup>1, 2</sup> Carnegie Mellon University
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## Abstract

2	Web-based eye-tracking is more accessible than ever. Researchers can now carry out
3	visual world paradigm studies remotely and access never before tested, multilingual
4	populations via the internet all without the need for an expensive eye-tracker. Web-based
5	eye-tracking, however, requires careful experimental design and extensive data wrangling
6	skills. In this paper, we provide a framework for reproducible, open science visual world
7	paradigm studies using online experiments. We provide step-by-step instructions to building
8	a typical visual world paradigm psycholinguistics study, and walk the reader through a series
9	of data wrangling steps needed to prepare the data for visualization and analysis using the
10	open-source software environment, R. Importantly, we highlight the key decisions
11	researchers need to make and report in order to reproduce an analysis. We demonstrate our
12	approach by carrying out a single change replication of an in-person eye-tracking study,
13	Porretta et al. (2020). We conclude with best practices and recommendations for researchers
14	carrying out bi-/multilingualism web-based visual world paradigm studies.
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16	Keywords: web-based eye-tracking, visual world paradigm, open science, data quality,
17	replication
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### 1. Introduction

2 Bi-/Multilingual psycholinguistic research is fundamentally constrained by the populations we can test and traditional lab-based research has tested university-aged adults 3 within Western, Educated, Industrialized, Rich, and Democratic (WEIRD) societies. 4 5 Whereas this lab-based approach undoubtably advanced psycholinguistics as a field, there 6 are at least two problems as a result. First, the field struggles to account for individual differences (e.g., Cunnings & Fujita, 2021). This is a natural limitation of largely testing 7 8 homogenous 18-to-30-year-olds. Yet, researchers continue to probe relationships between 9 speakers, their environment, and their cognition (Kidd et al., 2018, Perpiñán & Montrul, 10 2023). Second, the field has unintentionally promoted problematic methodological control in many bi-/multilingualism studies (Rothman et al., 2023). Bi-/multilingual studies, for 11 12 example, tend to compare 'monolinguals' to 'bilinguals' or 'natives' to 'non-natives.' Yet, notions of 'nativeness' or 'bilingualism' naturally vary given the study and setting (Brown 13 14 et al., 2022, Han et al., 2023).

Fortunately, web-based research has proliferated, thus removing geographical 15 16 barriers and allowing researchers to collect data from any population of languages users with access to the internet. This in turn allows bi-/multilingualism researchers the potential 17 to recruit more varied populations in search of individual differences and exert more 18 19 appropriate (theory-driven) experimental control in bi-/multilingualism research. Here we 20 discuss web-based visual world eye-tracking, which has become more accessible and reliable than ever (e.g., Semmelmann & Weigelt, 2017; Vos et al., 2022). Access to this 21 method, however, comes at the cost of multipart data wrangling to properly handle 22 between-participant differences in camera/browser specifications (Prystauka et al., 2023; 23 24 Vos et al., 2022).

As web-based eye-tracking grows in accessibility and popularity, it is essential to recognize that data wrangling is data analysis; it is data clean-up, transformation in and between data sets, visualization, and statistical analysis (Wickham & Grolemund, 2017). The choices made during web-based eye-tracking data wrangling can and should be standardized and reported, where possible, which in turn can help improve replicability and reliability in the field (e.g., Bolibaugh et al., 2021; Coretta et al., 2023). Here, we

1 provide a framework for handling multilingual web-based visual world paradigm eye-

- 2 tracking data using R (R Core Team, 2022).
- 3 1.1 The Visual World Paradigm

The visual world paradigm (VWP) involves displaying visual stimuli including a 4 5 target, and competitor(s), and/or distractor(s) with a variety of possible layouts and formats, 6 from pictures to words (e.g., Allopenna et al., 1998; Cooper, 1974; Tanenhaus et al., 1995). 7 While the images are shown, eve-movements are recorded and an audio stimulus (e.g., "beaker") is played aloud. The participant either needs to select the correct answer based on 8 9 the perceived audio or simply listen and look as the sound stimulus plays (e.g., passive 10 listening). VWP experiments vary widely in what linguistic process is being investigated e.g., referent prediction, sentence processing, word recognition, phonetic cue integration. However, 11 12 all VWP experiments carefully control three core constructs-time, audio stimuli, visual 13 stimuli—in order to bring meaning to a fourth core construct: eye-fixations. For the remainder of this paper, these "core four" constructs will be used to guide the reader's understanding of 14 15 how variation in eye-movement behavior can be captured, organized, and analyzed.



Figure 1. Illustration of the core four constructs within the VWP. Eye fixations,
represented by red dots, and respective times (blue dots).

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#### 5 *1.2 The Core Four Constructs of a VWP Experiment*

6 Time. Eye-tracking is especially valuable because it provides insight into the time-7 course of cognitive processing. Time can be measured from the beginning of the trial to the 8 end of the trial ('Trial Time' in Figure 1). There are two adjustments, however, that are typically made ('Adjusted Time' in Figure 1). First, it typically takes a listener about 200ms to 9 10 plan an eye-movement (Matin et al., 1993). Eye-movements within the first 200ms are 11 therefore discarded and researchers typically adjust their analysis accordingly. Second, within 12 each trial there exists a window of interest (grey area in Figure 1), which contains the crucial 13 information necessary to identify the target. For example, time in which any carrier phrase is 14 presented is typically ignored and time after the start of the target word is examined.

Audio Stimuli. The stimulus can be a word, a sentence, or even a non-speech noise.
 The audio informs the participant about the visual stimuli, often indicating which on-screen
 visual stimulus is the target or topic of the sentence. The audio stimuli must be carefully
 locked to time. For example, the end of the gold audio stimuli in Figure 1 is time-locked to
 end at 800ms (trial time).



Figure 2. Example visual stimuli inspired by Allopenna et al. (1998): target 'beaker',
onset competitor 'beetle', rhyme competitor 'speaker', and distractor 'stroller'.

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10 Visual Stimuli. Visual stimuli (Figure 2) can be presented with a preview time or simultaneously with the audio stimuli (Apfelbaum et al., 2021). Ultimately, the specific timing 11 used in a study depends on the research question. Most commonly, visual stimuli are made up 12 13 of two types: targets and competitors. In the case of four visual stimuli, an additional two visual stimuli can include a second competitor, a single distractor, two distractors, or even 14 target absent designs (Huettig & McQueen, 2007). Visual stimuli are always counterbalanced 15 16 across the four quadrants so as to reduce the chances of bias in eye-movements in a particular direction. Quadrants are absolute positions on the computer screen (e.g., upper right, bottom 17 18 left).

Eye-Fixations. Eye-fixations are time-stamped x- and y- screen coordinates that are
recorded throughout a trial i.e., where a participant is looking at a particular time. In Figure 1,
red dots are specific x- and y- coordinates and red lines tie those fixations to specific times

(blue dots). The rate of recording is a function of the measurements recorded per second (e.g.,
 measuring 1000 times in one second = 1000Hz). Eye-fixations get categorized into absolute
 positions on the screen (quadrants) and then mapped to visual stimuli. Where a participant is
 looking over time is informed by the audio stimuli.

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## 2. Building a Web-based Visual World Paradigm Experiment

Web-based eye-tracking experiments can be built with a variety of tools including
simple web-based GUIs, such as Gorilla/Pavlovia, as well as manual coding on Gorilla or
PCIbex Farm, or directly hosting a JavaScript-based experiment online. Readers are invited to
follow along on OSF with our detailed Gorilla tutorial (and cloneable experiments). Figure 3
shows an example of a single eye-tracking experiment trial.

Most eye-tracking experiments can be thought of as a forced-choice task (see Experimental ET Tasks for example: simple forced-choice at Gorilla link). From the participant's perspective, they hear an audio stimulus and select one of the visual stimuli<sup>1</sup>. Timing between the onset and/or offset of the core four constructs is essential: the audio and visual stimuli must be time-locked. When building the experiment, it is essential to focus on the timing of the trials, the types of data you want out of the trial<sup>2</sup>, and when the webcam should record eye-fixations.

<sup>&</sup>lt;sup>1</sup> Look and listen paradigm experiments are similar; however, no overt selection occurs.

<sup>&</sup>lt;sup>2</sup> Feedback is often used in bi-/multilingual studies; an additional *screen* indicating the correct target, such as a circle around the beaker or written corrective feedback could be added.





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Figure 3 shows how the exact presentation of your audio stimuli depends on where 5 6 you want the audio time-locked to the visual stimuli, which is determined by the respective 7 research question. For example, if we were to play the audio in Figure 2 in order to understand spoken word recognition (e.g., Allopenna et al., 1998), we would first show the 8 9 images and start the beginning of the audio stimulus at a set time after the visuals have been displayed (e.g., 200ms). In this way, participants' eye-fixations for the first 200ms would be 10 11 evenly distributed over the visual stimuli. Then as the word starts to play, the fixations would 12 gravitate towards the target (i.e., "beaker") and/or competitors (i.e., "speaker" and "beetle") and away from the distractor ("carriage"). As the trial progresses the fixations would tend 13 more and more toward the "beaker." 14

Most web-based eye tracking studies, including the current study, capture eyefixations using WebGazer.js (Papoutsaki et al., 2016). WebGazer.js is java script library that uses common webcams to infer the gaze of participants in real time. WebGazer is straightforward to use in both the self-hosted JavaScript based experiments as well as through Gorilla, Psychopy, and PCIbex. Best of all, many of the height and monitor restrictions used in in-person eye-tracking can be ignored because WebGazer uses ridge regression models to infer gaze under a variety of different user set-ups and behaviors.

1	When creating a WebGazer eye tracking experiment, either a five- or nine-point
2	calibration can be used, with any level set for calibration fail points or repeat calibrations.
3	Nine-point calibration provides a better standard but takes longer and may fail more often.
4	Although it is not necessary because of the manner in which WebGazer.js functions (Chen et
5	al., 2001), we recommended calibration at the beginning of the experiment with reported
6	calibration metrics provided. Importantly, webcams have variable frame-rates (frames per
7	second or FPS) that depend on participant movement, and the participant's device, which can
8	range between 20Hz and 60Hz (Vos et al., 2022). The typical raw eye-fixation samples
9	captured per second is 15, 30, 60, and 120 (standard webcam FPS) but will likely be much
10	lower in the actual data due to the aforementioned reasons.

Additionally, the participant's lighting environment can affect the number of fixations 11 12 recorded. For example, darker rooms may lower FPS. This means that some trials will capture 13 more/less eye-fixations than other trials (Prystauka et al., 2023). Whereas brighter rooms can 14 result in greater FPS, the directionality of the lighting can also affect calibration. If a light 15 source is behind the participants this can lead to improper exposure. Finally, the timing of eye-fixations can vary within a trial with non-equal measurements between captured eye 16 fixations. This means that the eye-fixations being captured start to drop throughout the trial. 17 This variability in frame-rate can be somewhat attenuated by doing in-person eye-tracking 18 19 with WebGazer but is nonetheless somewhat unavoidable (e.g., Papoutsaki et al., 2016).

20 2.1 VWP Raw Data and Tidy Data

Raw web-based eye-tracking data will vary given the platform for data collection (e.g.,
directly hosting or Gorilla). Raw data from a web-based VWP experiment, generally, has two
basic parts: behavioral task data and eye-tracking data (WebGazer data). Behavioral data will
include all selections and timings of those selections (e.g., reaction time, condition, trial

1 order). Eye-fixation data will contain trial-by-trial eye-fixation data that is paired with within-

### 2 trial trial-time.

					Λ	Eye-t	racking da	ta (1 particip	ant x a sing	le trial)
						ID	Trial	Time	Screen location x	Screen location y
		Tas	k data	1				Trial Time	Eye-fi	ations
ID	Trial	Audio file	Response	Correct		1	1	0.01	0.576	-0.236
		Audio Stimuli	Visuali stimuli selected			1	1	0.029	0.592	-0.222
1	1	beaker.wav	image_1	1		1	1	0.038	1.067	0.986
1	2	stroller.wav	image_3	1		1	1	0.082	1.13	0.852
2	1	beatle.wav	image_4	0			1			
2	2	speaker.wav	image_1	1						

3

4 Figure 4. Behavioral task data (left) and trial-specific eye-tracking data (right).

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6 The data structure depicted in Figure 4 is relational. That is, for every trial of each 7 participant, there exists a corresponding set of eve-tracking data that is associated with both the trial and the participant. The eye-tracking data provides a detailed account of the gaze 8 9 locations throughout the duration of the trial. This form of data while maximally informative, 10 is untidy and difficult to understand. We next turn to tidying the data so that each column refers to a single variable (e.g., audio stimuli) and each row is exactly one observation (e.g., 11 12 "beaker.wav"). In order to better demonstrate this process, we walk the reader through a replication study involving predictive sentence processing of accented and unaccented speech. 13 14

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### 3. Replication of Porretta et al. (2020)

### 16 *3.1 Background and Motivation*

We carried out a single change (web-based data collection) replication study of
Porretta et al. (2020)'s in-person VWP experiment. The study was chosen for replication for
two principled reasons following Marsden et al. (2018): 1) The majority of materials were

made available by the researchers, which minimizes heterogeneity. 2) The recency, novelty,
and theoretical impact of the initial study warrant replication for the sake of validation and
generalizability. Whereas our study changed only the method of collecting data, this single
change caused three important differences summarized in Table 1.

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**Table 1.** *Key Differences Between our Web-based Replication Study and Lab-based Porretta et al. (2020).*

8 9 —		Our web-based replication	Porretta et al. (2020)
10	Eye-tracker	Variable personal webcams	Eyelink 1000
11	Participants	60 Prolific participants	60 university students
12 13 —	Data wrangling	Self-wrangled	Pre-processed
14			

Porretta et al. (2020) used a 2-by-2 experimental design to manipulate talker (native/non-native) and verb type (restrictive/non-restrictive, e.g., "the fireman will climb/need the ladder", *climb* allows for object prediction but *need* does not). These English sentences were spoken by either a native or Chinese-accented talker. There were two research questions: 1) To what extent do restrictive and non-restrictive verbs modulate predictive sentence processing in accented and unaccented speech? 2) To what extent does accent experience modulate prediction in accented speech?

A direct comparison can be made between our study and Porretta et al. (2020) for research question one, which will indicate the usefulness of web-based eye-tracking for capturing prediction in sentence processing. For research question two, our interpretation will be limited given our random sample of Prolific participants (i.e., we are not controlling experience with Chinese-accented English). For this reason, results of the second analysis cannot provide insight into the quality of online eye-tracking data, but our approach may

instead provide evidence of the usefulness of web-based eye-tracking for recruiting varied,
 non-WEIRD populations outside the university setting, which may be particularly useful for
 advancing bi-/multilingualism psycholinguistics research and exploring individual
 differences.

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6 *3.2 Methods* 

We used Gorilla Experiment Builder's eye-tracking 2 zone implemented with
WebGazer.js (Anwyl-Irvine et al., 2019; Papoutsaki et al., 2016). <u>All research materials, R</u>
<u>data analysis, Gorilla experiment and tasks, and data are available on the Open Science</u>
<u>Framework</u> (OSF) (Foster & Deardorff, 2017). The study was approved by the authors'
Institutional Review Board. All participants were compensated for their participation. Average
completion time of the experiment was 16 minutes including a second (pilot) task that is not
reported here.

14

### 15 *3.2.1 Participants*

To ensure direct comparison to Porretta et al. (2020), we tested the same number of 16 participants, 60 (median age = 31). We recruited through Prolific (Palan & Schitter, 2018) 17 using the same criteria: native monolingual English speakers, between the ages of 18 to 40. 18 19 Not included in the 60 participants that completed the study were 37 rejected participants (eight failed headphone check, 23 failed eye-calibration, 5 timed-out after 90 minutes, one 20 21 failure to consent). As we demonstrate below, an additional 11 participants were removed 22 during the data tidying, resulting in 49 total participants analyzed. We return to this internet data quality issue and reduced statistical power in the discussion. 23

### 1 *3.2.2 Materials*

All recordings were taken from Porretta et al. (2020). The experiment contained 250 images, 50 of which were center images and 200 that made up targets and distractors. 99 of the images were identical to the original experiment (all 50 center images and 49 of the visual stimuli for objects across practice, filler, and experimental items). The remaining 151 images were obtained following the same specifications of the initial study (open-source line-drawn images). Four of the images were created in-house due to not being available online. Four presentation lists were made which counterbalanced talker and verb type.



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15 After consenting, each participant did two headphone checks: a basic listening task for

volume and a dichotic pitch task (Milne et al., 2021). Next, participants did a 5-point eye-

17 calibration set to reject participants below four successful points with a limit of three

- 18 calibration attempts before rejection. On each trial (24 target, 24 filler), participants were
- 19 presented with a 500-ms fixation cross followed by a 2x2 visual stimulus with an additional
- 20 center image that represented the subject of the sentence (Figure 5). Each stimulus was

Figure 5. Example Porretta et al. (2020) visual stimuli and center image. Restrictive
 sentences (e.g., the fireman climbed the ladder) or nonrestrictive (the fireman needs the

<sup>12</sup> *ladder*) sentences are counter balanced across participants.

<sup>14</sup> *3.2.3 Procedure* 

1 previewed for 200ms. Next, participants heard either a restrictive (e.g., the fireman climbed 2 the ladder) or nonrestrictive (the fireman needs the ladder) sentence spoken with either a native accent or non-native accent. Note competitors and distractors are conflated in this study 3 4 i.e., everything that is not the target (e.g., the ladder) could be considered a competitor or distractor. Participants then answered a simple comprehension question to ensure attention. 5 6 After the experimental task, participants filled out a brief questionnaire (identical to Porretta et al.'s) including age, language experience, and estimated Chinese accent experience 7 8 (captured on a scale of 0-100 with a slider that starts at zero). In order to make a comparison 9 to Porretta et al.'s reported mean of 1.78 (SD = 0.82), accent experience was scaled to 0-30and then log transformed with a constant of 1. Our population's mean of 0.99 (SD = 0.92), 10 therefore, is lower than that of Porretta et al.'s. 11

## 1 *3.3 Data Analysis*

2	In what follows, "L: + line number" (e.g., L:156-157) refer to line numbers in					
3	AOW_r_work_flow.rmd found on OSF. In L:33, we read in three data frames: The task_data,					
4	eye_tracking_data, and OSF_data. To follow along, download the data folder from OSF					
5	and select task_data.csv when prompted by R after running L:33. You can load the other data					
6	frames by running the following lines. Following Figure 5, the task_data is made up of the					
7	behaviora	I data and information obtained during testing; the eye_tracking_data is made up				
8	of eye-fix	ations. task_data is a messy 97,827 rows by 111 columns, and				
9	eye_trac	cking_data is an overwhelming 400,305 rows by 36 columns. As noted earlier, the				
10	data are r	elational. In the next 200 lines of code, we wrangle these structures into data that we				
11	can fully use, adapt, and share (see supplementary combining_data.Rmd for three methods					
12	on combining separate experimental files into a single data frame).					
13						
14	31	##Data Reading				
15	32	#select task_data				
16	33	<pre>task_data_select&lt;-file.choose()</pre>				
17	34	task_data<-read.csv(task_data_select,header=TRUE, row.names=1)				
18	35	#change for ET data				
19	36	et_data_select<-sub("task_data", "et_data", task_data_select)				
20	37	eyetracking_data<-read.csv(et_data_select,header=TRUE, row.names=1)				
21	38	#change for OSF data				
22	39	OSF_data_select<-sub("task_data", "OSF_data", task_data_select)				
23	40	OSF_data<-read.csv(OSF_data_select,header=TRUE, row.names=1)				
24						

## 25 *3.3.1 Questionnaire wrangling*

After loading all relevant packages and data, data wrangling always starts with data
removal. In a VWP experiment, removal occurs at four levels: questionnaire-based, item-

1	base	d, behavior-based, fixation-quality-based. Which level you start with is unimportant; we					
2	start with questionnaire-based removal and ask which participants should be excluded based						
3	on p	on post-experiment questionnaire exclusion criteria, which may be most relevant for bi-					
4	/mul	tilingualism studies (e.g., not an L1 English speaker and not between the ages of 18 and					
5	40).	In L:43, we start with a clone of our behavioral data frame task_data and assess needed					
6	varia	bles (Screen.Name, Responses, Participant.Private.ID, Reaction.Time(RT)). RT					
7	is ke	pt because it allows for removing items that were unnecessarily generated from the					
8	expe	riment structure (i.e., getting rid of rows with 0 RT).					
9							
10	42	##Questionnaire: Clean					
11	43	cleaned_quest_data<-task_data%>%					
12	44	<pre>filter(display=="questionairre",na.omit=TRUE)%&gt;%</pre>					
13	45	<pre>select(Participant.Private.ID,Screen.Name,Response,Reaction.Time)%&gt;%</pre>					
14	46	<pre>filter(Response != "",Reaction.Time!=0)%&gt;% select(!Reaction.Time)</pre>					
15							
16	Now	that we have a data frame with three columns (Participant.Private.ID,					
17	Scre	en.Name, Response), we can create tidy data with one observation per row and one					
18	varia	ble per column. pivot_wider() and pivot_longer() offer a simple solution to this					
19	com	mon data structure problem. Figure 6 demonstrates how experimental data (e.g., Gorilla-					
20	tasks, Psychopy, E-Prime) often require widening, whereas questionnaire data (e.g., Gorilla-						
21	questionnaires, Google forms, Qualtrics) require pivoting longer. In L:49, we pivot wider to						
22	create a single row for each participant with each question having its own column. It is much						
23	easier to come up with standards for removal in the speaks_L2, age, or hear_impaired						
24	columns than for the Response column, which would require conditional standards based on						
25	Scre	en.Name.					

1	49	##Questionnaire: Tidy
2	50	tidy_quest_data<-cleaned_quest_data%>%
3	51	group_by(Participant.Private.ID,Screen.Name)%>%
4	52	<pre>summarise_all(toString)%&gt;%</pre>
5	53	<pre>pivot_wider(names_from=Screen.Name,values_from=Response)%&gt;%</pre>
6	54	<pre>mutate(speaks_L2 =if_else(str_detect(other_languages_spoken,"German")&amp;</pre>
7	55	<pre>!is.na(other_languages_spoken),1,0),</pre>
8	56	<pre>across(c(chinese_study_duration,age,experience_chinese_accent),</pre>
9	57	as.numeric),
10	58	<pre>Participant.Private.ID = as.factor(Participant.Private.ID))%&gt;%</pre>
11	59	<pre>select(!other_languages_spoken)</pre>

12

ID	screen.Name	response			
1	age	24			
1	speaks_L2	1			
1	hear_impaired	0		_	
2	age	36			
2	speaks_L2	0	ID	age	speaks L2
2	hear_impaired	0		- ge	opounto
00001			1	24	1
_onger			2	36	0

13

14 Figure 6. Examples of long data (left) and wide data (right).

- In L:69, we find that two participants should be removed for language expertise
  outside English and one for exceeding the age cutoff (both predetermined values based on
  Porretta et al.). We can now use this data frame to filter out unqualified participants in the
  Participant.Private.ID column of the next removal stage (See L:61-68 in
- 20 AOW\_r\_work\_flow.rmd for an example of helpful visualization).

1	69	##Questionnaire: Filtered
2	70	filtered_quest_data<-tidy_quest_data%>% filter(age<=40
3	71	& age>=18, #1 removed for age range
4	72	chinese_study_duration==0, <pre>#none removed</pre>
5	73	<pre>speaks_L2==0,#2 removed that speak other languages</pre>
6	74	<pre>language_disorder == "No") #none removed</pre>

7

## 8 *3.3.2 Behavioral-task wrangling*

9 The next cycle of data wrangling begins with the question: Which participants and items should be removed based on the behavioral results? Cleaning is similar to the 10 11 questionnaire cycle, but we start from scratch with a clone of task data called 12 experimental cleaned because the new question has new goals, which requires different variables. We start this cycle's implementation by filtering the participants in the behavioral-13 task clone with the questionnaire data from above in order to only keep those participants that 14 15 qualified in the questionnaire wrangling cycle (L:77). We then remove all rows except ones 16 related to behavioral data questions (L:78-79) and experimental items (L:80), followed by 17 removing columns with all NAs. Lastly, to achieve tidy data, we split the visual image selection and comprehension question into two columns so that each participant has a single 18 19 observation for each trial (e.g., pivot into a wider structure, L:84). Removal of columns in 20 L:86-88 makes pivoting possible. Pivoting requires that rows do not have uniquely 21 identifiable information outside the data columns being "widened" (This could also be achieved with the column argument of pivot wider). 22

1	76	##Experimental Data: Clean and Tidy
2	77	experimental_cleaned <- task_data%>%
3	78	filter(Participant.Private.ID %in%
4	79	filtered_quest_data\$Participant.Private.ID)%>%
5	80	<pre>filter(Zone.Type == "response_button_image")</pre>
6	81	<pre>Zone.Type == "response_button_text")%&gt;%</pre>
7	82	<pre>filter(verb_type == "Restricting"  verb_type == "NonRestricting")%&gt;%</pre>
8	83	<pre>select_if(~sum(!is.na(.)) &gt; 0)</pre>
9	84	
10	85	experimental_tidy<-experimental_cleaned%>%
11	86	<pre>select(!c(Event.Index:Local.Date,</pre>
12	87	Screen.Number:Zone.Name,
13	88	Reaction.Time:Response.Type))%>%
14	89	<pre>pivot_wider(names_from = Zone.Type,values_from = Response)%&gt;%</pre>
15	90	<pre>mutate(subject_img_file=center_image)#for renamed match in next step</pre>
16		
17		Additionally, we must load in a second data frame $osf_data$ (L:94) from the original
18	expe	riment. We do this because our experiment only has the quadrants or the visual stimuli
19	with	out the target, competitor, and distractor information, and later we need SUBTLWF_obj,
20	whic	h is the log frequency of the object words used in the statistical models.
21		
22	93	##OSF Data: Clean and Tidy
23	94	OSF_filt<-OSF_data%>%
24	95	<pre>select(talker,verb_type,subject_img_file,img_1_file, img_2_file,</pre>
25	96	<pre>img_3_file, img_4_file,log_SUBTLWF_Obj)</pre>
26		
27		In L:99, we filter the OSF_data for experimental items and use a left_join() based
28	on ta	lker condition verb_type, and the center visual image subject_img_file, which
29	simu	ltaneously pulls in the variables that we need and filters out nonce items (this step could

1 be avoided by putting these variables in the original experimental spreadsheets). Figure 7

2 demonstrates filtering through different types of joining.

3						
4	<pre>4 98 ##Behavioral Data: Join OSF and Experimental Data 5 99 behavioral_data&lt;-experimental_tidy%&gt;% 6 100 left_join(OSF_filt, by=c( "talker", "verb_type", "subject_img_file")) 7</pre>					
5						
6						
7						
		Inner join	Left join	Right join	Outer/Full join	
8 9 10 11 12 13 14	<b>Figu</b> fram fram left jo both	<b>re 7.</b> Solid portions i es. Left join is more i e and matching value oin. Inner join is the data frames.	refer to what is kept. Fu restrictive and includes es from the right data fi most restrictive, it only	all join retains all rows f all the rows from the le rame (second). Right jou retains rows with match	from both data ft (first) data in is the inverse of hing values from	
15		Now that we have	the variables we need i	${f n}$ behavioral_data, w	e can create variables	
16	for th	ne answers being cor	rect/incorrect for our re	moval process. We will	do this for both the	
17	item	selection (L:105) and	d comprehension quest	ion (L:106).		
18						
19	102	##Behaviora	l Data: Clean and S	Fidy		
20	103	behavioral_data	<-behavioral_data	8>8		
21	104	mutate(partic	ipant = as.factor(1	Participant.Private	.ID),	
22	105	image_in	correct= if_else(ir	ng_1_file==response	_button_image,0,1),	
23	106	text_inc	orrect = if_else(re	esponse_button_text	=="Yes",0,1))	
24		Importantly, resea	rchers should establish	a criterion for removal	prior to data	
25	colle	ction. Because Porre	tta et al. (2020) did not	report the criteria they	used, we based our	

1 removal on three standard deviations from the mean inaccuracy of participants/items

2 separately, which results in three participants being removed.

```
3
     108 ## ----Behavioral Data: Removal Standards----
 4
 5
     109 #Standard deviations is used to retain maximum amount of quality data
     110 #We set all of these to be 3 SDs, code here is only for your future use
 6
     111 image participant threshold = 3
 7
     112 image item threshold = 3
 8
     113 text participant threshold = 3
 9
     114 text_item threshold = 3
10
11
            We aggregated participant inaccuracies by adding together incorrect items by
12
     participant and item for both item selection (L:118-129) and comprehension question (L:131-
13
     142), respectively. We end here by removing the incorrect trials to prepare for the eye-tracking
14
15
     data wrangling (L:144-145).
```

1	116	##Behavioral Data: Participant and Item Removal
2	117	#participant removal
3	118	participant_agg<-behavioral_data%>%
4	119	group_by(Participant.Private.ID)%>%
5	120	<pre>summarize(num_incorrect_image=sum(image_incorrect),</pre>
6	121	<pre>num_incorrect_text=sum(text_incorrect))%&gt;%</pre>
7	122	<pre>mutate(mean_image_score = mean(num_incorrect_image),</pre>
8	123	<pre>sd_image_score = sd(num_incorrect_image),</pre>
9	124	<pre>mean_text_score = mean(num_incorrect_text),</pre>
10	125	<pre>sd_text_score = sd(num_incorrect_text))%&gt;%</pre>
11	126	filter(num_incorrect_image <= mean_image_score+
12	127	(sd_image_score*image_participant_threshold) $\&$
13	128	<pre>num_incorrect_text &lt;= mean_text_score+</pre>
14	129	(sd_text_score*text_participant_threshold))
15	130	#item removal
16	131	item_agg<-behavioral_data%>%
16 17	131 132	<pre>item_agg&lt;-behavioral_data%&gt;% group_by(center_image)%&gt;%</pre>
16 17 18	131 132 133	<pre>item_agg&lt;-behavioral_data%&gt;% group_by(center_image)%&gt;% summarize(num_incorrect_image=sum(image_incorrect),</pre>
16 17 18 19	131 132 133 134	<pre>item_agg&lt;-behavioral_data%&gt;% group_by(center_image)%&gt;% summarize(num_incorrect_image=sum(image_incorrect),</pre>
16 17 18 19 20	131 132 133 134 135	<pre>item_agg&lt;-behavioral_data%&gt;% group_by(center_image)%&gt;% summarize(num_incorrect_image=sum(image_incorrect),</pre>
16 17 18 19 20 21	131 132 133 134 135 136	<pre>item_agg&lt;-behavioral_data%&gt;% group_by(center_image)%&gt;% summarize(num_incorrect_image=sum(image_incorrect),</pre>
16 17 18 19 20 21 22	131 132 133 134 135 136 137	<pre>item_agg&lt;-behavioral_data%&gt;% group_by(center_image)%&gt;% summarize(num_incorrect_image=sum(image_incorrect),</pre>
16 17 18 19 20 21 22 23	131 132 133 134 135 136 137 138	<pre>item_agg&lt;-behavioral_data%&gt;% group_by(center_image)%&gt;% summarize(num_incorrect_image=sum(image_incorrect),</pre>
16 17 18 19 20 21 22 23 24	131 132 133 134 135 136 137 138 139	<pre>item_agg&lt;-behavioral_data%&gt;% group_by(center_image)%&gt;% summarize(num_incorrect_image=sum(image_incorrect),</pre>
16 17 18 19 20 21 22 23 24 25	131 132 133 134 135 136 137 138 139 140	<pre>item_agg&lt;-behavioral_data%&gt;% group_by(center_image)%&gt;% summarize(num_incorrect_image=sum(image_incorrect),</pre>
16 17 18 19 20 21 22 23 24 25 26	131 132 133 134 135 136 137 138 139 140 141	<pre>item_agg&lt;-behavioral_data%&gt;% group_by(center_image)%&gt;% summarize(num_incorrect_image=sum(image_incorrect),</pre>
16 17 18 19 20 21 22 23 24 25 26 27	131 132 133 134 135 136 137 138 139 140 141 142	<pre>item_agg&lt;-behavioral_data%&gt;% group_by(center_image)%&gt;% summarize(num_incorrect_image=sum(image_incorrect),</pre>
16 17 18 19 20 21 22 23 24 25 26 27 28	131 132 133 134 135 136 137 138 139 140 141 142 143	<pre>item_agg&lt;-behavioral_data%&gt;% group_by(center_image)%&gt;% summarize(num_incorrect_image=sum(image_incorrect),</pre>
<ol> <li>16</li> <li>17</li> <li>18</li> <li>19</li> <li>20</li> <li>21</li> <li>22</li> <li>23</li> <li>24</li> <li>25</li> <li>26</li> <li>27</li> <li>28</li> <li>29</li> </ol>	131 132 133 134 135 136 137 138 139 140 141 142 143 144	<pre>item_agg&lt;-behavioral_data%&gt;% group_by(center_image)%&gt;% summarize(num_incorrect_image=sum(image_incorrect),</pre>

1		One important note here is that the removal is done in parallel. That is, we removed	
2	participants and items simultaneously. If you sequentially remove participant or item first ther		
3	remo	val results would be different in the behavioral_data (e.g., more or less items or	
4	partic	cipants would be removed). Said another way, this removal method assumes that a "bad"	
5	item	or poor performing participant would be below the distributional counts independently.	
6			
7	3.3.3	Eye-tracking wrangling	
8		Removal and adjustment of eye-tracking data is done through an exploratory lens as	
9	there	is little current reference for expected results for eye-fixations and frame-rate in web-	
10	based eye-tracking. However, recent work has begun to fill this gap (see Prystauka et al.,		
11	2023; Vos et al., 2022). Here, two questions guide our approach: How should eye-fixations be		
12	classified into quadrants in web-based eye-tracking? And, what quality of frame-rate is		
13	needed to capture the effects of interest? We start by filtering out participants from the		
14	previous data sets. Here, the retained participants (L:118) and items (L:131) from the previous		
15	step a	are used to define what we want to keep in the behavioral_data (L:148-150) with	
16	the %	in% operator.	
17			
18	147	##Behavioral Data: Removing with IN Operator	
19	148	behavioral_data<-behavioral_data%>%	
20	149	filter(Participant.Private.ID%in%	
21		participant_agg\$Participant.Private.ID&	
22	150	center_image %in% item_agg\$center_image)%>%	
23	151	<pre>select(-c(text_incorrect,image_incorrect,response_button_text))</pre>	
24			

Whereas the et\_data is much larger than the previous data frames, the same methods
are used. Selection of data can be reduced to only the time time\_elapsed, participant

participant\_id, and eye-fixations x\_pred\_normalised y\_pred\_normalised (L:154-156),
 which is filtered by only usable fixation points (L:157), followed by variable renaming for
 upcoming joining of et\_data and behavioral\_data (L:158-159).

4

```
153 ## ----ET Data: Tidying and Filtering with an Inner Join---
 5
 6
     154 et data <- eyetracking data >>%
 7
            select(time elapsed,participant id,spreadsheet row,
     155
 8
     156
                    type,x_pred_normalised,y_pred_normalised) %>%
 9
            filter(type =="prediction" )%>%
     157
10
            rename("Participant.Private.ID"="participant id",
     158
11
                    "Spreadsheet.Row"="spreadsheet row")
     159
```

12

Now that both behavioral data and et data are cleaned and tidy, left join() 13 14 (L:173) is used to create all data from our behavioral data and eye tracking data. This data frame now has all of the eye-tracking data and behavioral-task data from the entire 15 experiment (L:173-174). However, the data from the et data only includes unclassified eye-16 17 fixations. Specifically, it includes the x and y coordinates without a link to the visual stimuli that are being viewed. A Shiny app was created to dynamically explore how eye-fixations are 18 distributed with variable amounts of removal at four crucial time points: the beginning of the 19 20 sentence (-400ms), verb onset (0ms), object onset, and selection of visual stimuli. The app also includes dynamically calculated data loss. Figure 8 is a fixed version of the fixation points from 21 22 the app (See Eye-fixations Shiny App in OSF). In the discussion, implications of removal standards based on eye-fixation alone are considered and discussed as a signal detection 23 problem. 24

As displayed in Figure 8, fixations are mostly distributed at the center of the screen, indicating no looks to quadrants. Whereas this remains true for competitor items throughout the

1 trial, target items begin to move toward visual stimuli as early as the verb onset and much more 2 in later time frames. Crucially, however, the fixations do not always reach the actual quadrants. In analyzing the data from the Shiny app, removing data between the center point of the screen 3 4 and the inner-edges of the quadrants results in ~83.33% data loss, which is more than twice as high as previously reported for two image web-based studies (Vos et al., 2022). If we move to 5 6 a more relaxed categorization, then only 6.71% of data is lost. In contrast, maximal outer-edge 7 removal results in very little data loss (max  $\sim$ 32%). When removing inner-edge eye-fixations, the choice comes down to removing signal to avoid noise in spatial ambiguity, or embracing 8 9 noise to maximally retain the signal. As shown in the competitors-time 800 (upper-right) section of Figure 8, the noise is randomly distributed across quadrants just as it is early in the trial 10 before eye-movements tend toward visual stimuli. Here, we aim to strike the balance of the 11 12 signal-to-noise trade off by removing most of the data outside the screen size and by maximally retaining inner data that shows trends. This leads us to believe that no bias would occur even if 13 classifying data from the x, y fixation center (0.5, 0.5). 14



15

**16** Figure 8. *Quadrant locations and actual screen sizes are denoted with white lines.* 

1 From L:180-190, we create a classification system based on no inner-edge removal of the eye-fixations and partial removal of outer-edge eye-fixations (the code was created with inner 2 removal in mind so that future researchers can simply adapt the distance variable L:177, if 3 4 desired). We use two types of control flow to first classify eye-fixations into quadrants and then create binary variables to link the quadrant to the visual stimuli. case when () is used 5 (L:180-190) because of the multiple conditions and because case when () is Boolean, 6 7 meaning it provides a specific output in the case of something being true. For example, if we 8 only want to classify images that are within a particular space and leave others blank, then 9 non-binary classification like case when () is optimal. In contrast, if the outcomes of a classification are binary, then ifelse() is an effective solution. For example, L:192-200 10 11 makes a binary decision on whether an image being viewed is the same or different from the target (L:193), competitors (L:194-195), and distractor (L:196), separately (Note that 12 competitors and distractors are the same in our experiment, so we included this for ease of 13 future use). While complexity of implementation may vary, logically either can be used to 14 15 achieve the same result in all cases with the use of operators and/or nesting.

1	171	##ET Data: Localizing Visual Stimuli		
2	172	#logically equivalent to doing full join and removing non-experimental trials.		
3	173	all_data <-behavioral_data %>%		
4	174	<pre>left_join(et_data, by=c("Participant.Private.ID", "Spreadsheet.Row"))</pre>		
5	175			
6	176	center=.5#center of screen		
7	177	distance=0#distance to visual stimuli		
8	178	<pre>beyond_screen=1 #distance to beyond_screen</pre>		
9	179			
10	180	all_data<-all_data%>%		
11	181	<pre>mutate(image_viewing=</pre>		
12	182	<pre>case_when(x_pred_normalised &lt;= center-distance &amp;</pre>		
13	183	<pre>y_pred_normalised &gt;= center+distance ~ image_1,</pre>		
14	184	<pre>x_pred_normalised &gt;= center+distance &amp;</pre>		
15	185	<pre>y_pred_normalised &gt;= center+distance ~ image_2,</pre>		
16	186	x_pred_normalised <= center-distance &		
17	187	<pre>y_pred_normalised &lt;= center-distance ~ image_3,</pre>		
18	188	<pre>x_pred_normalised &gt;= center+distance &amp;</pre>		
19	189	<pre>y_pred_normalised &lt;= center-distance ~ image_4))%&gt;%</pre>		
20	190	<pre>filter(!is.na(image_viewing))</pre>		
21	191			
22	192	all_data<-all_data %>%		
23	193	<pre>mutate(target = if_else(image_viewing == img_1_file, 1, 0),</pre>		
24	194	<pre>comp_1 = if_else(image_viewing == img_2_file, 1, 0),</pre>		
25	195	<pre>comp_2 = if_else(image_viewing == img_3_file, 1, 0),</pre>		
26	196	<pre>dist = if_else(image_viewing == img_4_file, 1, 0))%&gt;%</pre>		
27	197	filter(x_pred_normalised>center-beyond_screen &		
28	198	x_pred_normalised <center+beyond_screen&< th=""></center+beyond_screen&<>		
29	199	y_pred_normalised>center-beyond_screen &		
30	200	<pre>y_pred_normalised<center+beyond_screen)< pre=""></center+beyond_screen)<></pre>		



1



#### 4

Participants Ordered by Median Frame Rate

Figure 9. Participant frame-rate. Mean is marked with dotted horizontal line. High,
medium and low categories are defined by the median frame-rate of each participant,

*meaning and fow categories are defined by the meaning rame-rate of each participant, making cutoffs by peaks of the distribution. Frame is shown in hertz (Hz) and participants are individually represented by each boxplot.*

9

Like other recent web-based eye-tracking studies, our mean frame-rate was 20Hz (M = 10 22.17Hz, SD = 11.61). Here, we remove the five participants with less than 5Hz median 11 12 frame-rates and create time bins by first creating a standard for removal in L:378 and a binning size (L:379). Median is used because means are more sensitive outliers; e.g., if a 13 participant has one exceptionally low frame-rate this will not be just cause for removal if we 14 use medians (Leys et al., 2013). We then aggregate by participant Participant. Private. ID, 15 item subject img file, and condition verb type talker (L:381) in order to remove all 16 participants that are below our standard predetermined median; i.e., 5Hz (L:381-388) (Vos et 17 al., 2022). Next, time bins are created by normalizing the time range for each item (L:389). 18 19 Additionally, we subtracted 200ms for human eye movements to occur and thus center the time so that zero is always the onset of the verb of interest (this step was not explicit in 20

21 Porretta et al. (2020), but we recommend future researchers always make this step explicit to

```
1
     ensure that future studies can reproduce your results). After normalizing, bins are created by
 2
     dividing the time time elapsed by the bin size time binning, rounding, then multiplying
     by the bin size time binning (L:390), which is simply rounding items to the nearest bin size
 3
     number thus allowing you to use any size bin for your data rather than an assumed pre-set bin
 4
 5
     size.
 6
     377 ## ----All Data: Clean and Tidy---
 7
     378 frame rate cut off<-5
 8
     379 time binning<-50
 9
     380 all data cleaned<-all data%>%
10
             group by(Participant.Private.ID,subject img file,verb type,talker)%>%
     381
11
     382
             mutate(count = n()),
12
     383
                     max time = max(time elapsed),
13
                     frame_rate = count/max time*1000)%>%
     384
14
             ungroup() %>%
     385
15
     386
             group by(Participant.Private.ID)%>%
16
     387
             mutate(median frame rate = median(frame rate))%>%
17
     388
             filter(median frame rate>=frame rate cut off) %>%
18
             mutate(time elapsed=time elapsed-object start-200) %>%
     389
19
     390
             mutate(time elapsed rounded=time binning*round
20
                    ((time elapsed) / time binning))
21
     391
22
     392 all data tidy <- all data cleaned >>%
23
     393
             filter(time elapsed rounded>=-400 & time elapsed rounded<=800)
24
            Creating time bins is fundamentally discretizing a continuous scale. In any fixed set of
25
     eye-tracking data, the grain size of the time scale has an inverse relationship to the amount of
26
```

27 data in each time bin. If you increase the bin size, you will have more data per bin, but less

28 bins across time. Many statistical analyses can bypass the binning procedure altogether by

keeping time a continuous variable. Nevertheless, for analyses that do require time bins and
for visualization alone, it is worth exploring whether specific bin sizes affect a researcher's
ability to capture an effect. To do this, we created a second Shiny app that is depicted in
Figure 10 (see Frame-Rate Shiny App in OSF). The Frame-Rate Shiny App allows the reader
to explore the interactions between data removal based on participant median frame-rates,
changing bin sizes, and seeing output in the form of empirical logits for either linear lines or
GAMM smoothed curves. Here, two crucial discoveries are made.

First, almost any arbitrary sized bin captures the effect of verb\_type, with the caveat of
the bin needing to be several sizes smaller than the window of interest. Second, nearly any
frame-rate of data can capture the effect outside very low frame-rates of 5Hz and below. If
only examining data that is 6-11Hz, the effect of verb\_type for talker starts to become
apparent while the accented speaker effect for verb\_type becomes apparent between 12-17
Hz.

14



15

16 Figure 10. Total looks per bin size. Like figure 9, high, medium, and low categories are

17 *defined by the median frame-rate of each participant. Adjusted time is in milliseconds* 

<sup>18</sup> *(ms). Looks captured are raw counts across participants/items.* 

1 The last step before visualization and statistical analysis is a final tidying. Like the 2 first wrangling that we did, we create a tidy data frame through removal. Here, all evefixations that are outside the window of interest (-400ms and 800ms) are removed. Now, our 3 4 new tidy data is structured based on the core four constructs. For each participant, each audio stimuli and visual stimuli set is classified by talker and verb type. Finally, we have 5 removed all times outside the window of interest. By tidying in this way, eye-fixations 6 7 become meaningful in that each row is classified into looks to targets, competitors, and 8 distractors, and each row is a classified eye-fixation based on a specific time, for each 9 participant, and for varying conditions. Between the two data frames all data cleaned and all data tidy, we have all of the behavioral data ready for any analysis or exploration that 10 11 can be done. 12

- 13

## 4. Modeling ET data

14 In all previous steps, wrangling can be thought of as a condensing process, where the primary object is to remove, clean, and transform the data into a structure that is usable. 15 However, once the data is put into tidy form, then the data must be transformed for specific 16 visualizations and statistical analyses (hereafter, models). In this section, we think of 17 all data cleaned and all data tidy as launching points to gain an understanding of our 18 19 data<sup>3</sup>.

20 We start by creating two data frames from all data tidy : mem data in L:453 and 21 gamm data in L:459. In general, maximally retaining informative columns is essential to 22 creating a usable data frame. When building models, however, it is often best to remove

<sup>&</sup>lt;sup>3</sup> If you wish to start from here then read in the all data tidy and all data cleaned from cleaned data on OSF.

1	varia	bles that you will not be using. This is because some models can have complications	
2	interpreting unprocessed data types (e.g., NAs ). For mem_data, we start by selecting all		
3	neces	ssary columns for the model (L:454-455). Factor type conversion occurs next (L:456).	
4	Final	ly, to get background information we join tidy_quest_data. In addition to the	
5	mem_	data, we create gamm_data by simply cloning mem_data in L:459 and by adding a	
6	singl	e variable needed in the GAMM models.	
7	452	##All Data: Preparing for Models	
8	453	mem_data<-all_data_tidy%>%	
9	454	<pre>select(Participant.Private.ID,verb_type,talker,</pre>	
10	455	<pre>subject_img_file,target,Trial.Number,log_SUBTLWF_Obj,</pre>	
11		<pre>target_obj,time_elapsed)%&gt;%</pre>	
12	456	<pre>mutate(Participant.Private.ID=as.factor(Participant.Private.ID))%&gt;%</pre>	
13	457	<pre>left_join(filtered_quest_data)</pre>	
14	458		
15	459	gamm_data<-mem_data%>%	
16	460	<pre>mutate(Condition = paste(talker,verb_type,sep="."))</pre>	
17			

There are a handful of excellent papers that outline the advantages and disadvantages 18 of different methods of eye-fixation analysis and relevant considerations for each method of 19 20 analysis (Barr, 2008; Ito & Knoeferle, 2022; McMurray, 2023; Mirman et al., 2008). Here, we 21 continue to focus on the data wrangling process and present the data wrangling steps-and decisions-needed to carry out two of the more widely used statistical analyses in the field: 22 generalized linear mixed effect models (GLMMs) and generalized additive mixed effects 23 24 models (GAMMs), which does not require the assumption of linearity. Both GLMMs and 25 GAMMs require specific contrast coding (e.g., dummy, orthogonal) of the data before running models to get expected results. After contrast coding, all model building starts with maximal 26

models, as justified by the design, working down to simpler models for model comparison
(see Barr et al., 2013).

3

4 *4.1 GLMMs* 

```
5 4.1.1 GLMMs: coding
```

```
6
           For GLMMs coding, start with data type conversion (L:464-465), then re-level both
     talker (Native, Non-Native) and verb type (Restrictive or Non-Restrictive) so that
 7
     verb type Restrictive and talker Native are both set as reference levels (L:466-467). We
 8
 9
     can then rename the contrasts to improve model output readability (L:468-471) and later
     visualization. In L:473 through L:476, we normalize the time elapsed. Lastly, we create a
10
11
     data frame for the accent model (L:477).
     463 ## ----GLMM: Leveling the Data---
12
13
     464 mem data$verb type<-as.factor(mem data$verb type)
14
     465 mem data$talker<-as.factor(mem data$talker)
15
     466 contrasts(mem data$verb type) <-c(-.5,.5)
16
     467 contrasts (mem datatalker) <-c(-.5,.5)
17
     468 colnames(contrasts(mem data$talker))<- c('Native:')</pre>
18
     469 rownames(contrasts(mem data$talker))<-c("Native", "NonNative")
19
     470 colnames(contrasts(mem data$verb type)) <- c('Restricting:')
20
     471 rownames(contrasts(mem data$verb type)) <-
21
                              c("Non-Restricting", "Restricting")
22
     472 mem data$experience chinese<-mem data$experience chinese accent
23
     473 mem data <- mem data %>%
24
     474
             mutate(time normalized =
25
                    (time elapsed - min(time elapsed)) /
     475
26
                    (max(time elapsed) - min(time elapsed)))
     476
27
     477 accent mem data<-mem data%>%filter(talker == "NonNativeMale")
28
```

## 1 4.1.2 GLMMs: models

2	Two GLMMs were built using the lme4 package (Bates et al., 2014). Looks to the			
3	target (coded as 1, 0) served as the dependent variable. The Main Model included three fixed			
4	effects: verb_type (Restrictive or Non-Restrictive), talker (Native,			
5	Non-Native) and their interaction (L:509). Random intercepts for $subject_img_file$ ,			
6	Participant.Private.ID, and time_normalized were included, as were random slopes			
7	for talker and verb_type. The logit link function ("binomial") was specified in the model,			
8	equivalent to modeling logit-transformed response probability with identity link function.			
9	Model comparison <sup>4</sup> showed preference for the full model with ANOVA comparisons (p			
10	<.001) and lower AIC and BIC.			
11				
12	508 ##GLMM: Main Model			
13	509 glmm1_1<-glmer(target~talker*verb_type+			
14	510 (talker subject_img_file)+			
15	511 (verb_type Participant.Private.ID)+			
16	512 (1 time_normalized),			
17	513 family="binomial", data=mem_data)			
18	514 summary(glmm1_1)			
19				
20	Similar to the above model, an accent only model was run on accent_mem_data.			
21	Model specifications are identical to Main Model outside of changing fixed effects to			
22	experience_chinese (L:540). Additionally, talker is removed as a random slope			
23	because accent_mem_data only has one talker: accented. Full models were shown to			
24	outperform simpler models from ANOVA comparisons ( $p < .001$ ) and lower AIC and			
25	BIC, as well as non-convergence of simpler models.			

 $<sup>^4</sup>$  See <code>AOW\_r\_work\_flow.rmd</code> for all model comparisons

```
1
 2
     539 ## ----GLMM: Accent Model---
 3
     540 glmm2 1<-glmer(target~experience chinese+
 4
     541
                         (1|subject img file)+
 5
     542
                         (1|Participant.Private.ID) +
 6
     543
                          (1|time normalized),family="binomial",data=accent mem data)
 7
     544 summary(glmm2 1)
 8
 9
     4.2 GAMMs
           Like GLMM data, GAMM data must be first coded/prepared (L:546-559). Here, we
10
     turn variables into factors and level them at the same time (e.g., L:550-553). However, it is
11
```

12 important to note that GAMMs interpret sum-coded variables most effectively, L:550-552. We

13 create event as a combination between conditions (L:554-555). Then we only select()

14 columns necessary for the analysis (L:557-559). Lastly, we split off the accent data for the

15 accent GAMM (L:560).

1	546	##GAMM: Leveling the Data
2	547	gamm_data <- gamm_data %>%
3	548	mutate(
4	549	Condition = as.factor(Condition),
5	550	<pre>subject_img_coded = as.numeric(factor(subject_img_file)) - 1,</pre>
6	551	<pre>talker_coded = as.numeric(factor(talker)) - 1,</pre>
7	552	<pre>verb_type_coded = as.numeric(factor(verb_type)) - 1,</pre>
8	553	<pre>Participant.Private.ID = as.factor(Participant.Private.ID),</pre>
9	554	<pre>Event = as.factor(paste(</pre>
10	555	<pre>Participant.Private.ID,Trial.Number,sep= ".")),</pre>
11	556	<pre>experience_chinese = experience_chinese_accent)%&gt;%</pre>
12	557	<pre>select(Event,Participant.Private.ID,Trial.Number,verb_type_coded,</pre>
13	558	<pre>talker_coded,subject_img_coded,Condition,target,time_elapsed,</pre>
14	559	<pre>log_SUBTLWF_Obj,experience_chinese,Event)</pre>
15	560	<pre>gamm_data_accented&lt;-gamm_data%&gt;%filter(talker_coded == 1)</pre>
16		GAMM Models were built using the mgcv package (Wood, 2017). Model comparisons
17	sugg	est that random intercept of Event significantly improved the maximal model. Like the
18	GLN	IM model, the GAMM models treat looks to the target (L:603) as the dependent variable
19	with	independent variables including three fixed effects: talker_coded (L:603),
20	verb	o_type_coded (L:605) and their interaction (L:607). Random effects included Event
21	(L:6	12). Smooth terms were included for time_elapsed by levels of talker_coded (L:604),
22	verb	_type_coded (L:606), and Condition (L:608). Smooth terms allow for a non-linear
23	relat	ionship between time_elapsed and the response variable verb_type_coded, with a
24	diffe	rent smooth function for each level of variable. An additional smooth term for
25	log_	SUBTLWF_Obj (L:609) was included. Smooth terms for time_elapsed were included for
26	grou	ping levels: Participant.Private.ID and subject_image_file (L:610-611). The
27	logit	link function ("binomial") was specified in the model, equivalent to modeling logit-
28	trans	formed response probability with identity link function.

```
1
 2
     602 ## ----GAMM: Main Model---
 3
     603 mod1 <- bam(target ~ talker coded +
 4
     604
                      s(time elapsed, by=talker coded) +
 5
                      verb type coded +
     605
 6
     606
                      s(time_elapsed, by=verb_type_coded) +
 7
     607
                      talker coded:verb type coded +
 8
     608
                      s(time elapsed, by=Condition) +
 9
     609
                      s(log SUBTLWF Obj)+
10
     610
                      s(time elapsed, Participant.Private.ID, bs="fs", m=1)+
11
                      s(time elapsed, subject img coded, bs="fs", m=1)+
     611
12
     612
                      s(Event, bs="re"),
13
     613
                      family="binomial", data=gamm data, discrete=TRUE, method="fREML")
14
     614 summary (mod1)
15
            The accent GAMM had identical structure to the main GAMM with the expectation of
16
     having only 1 main effect, experience chinese (L:642), and removing the smoothing term
17
     leveled by talker coded. gamm data accented was the data frame (L:648). Model
18
     comparisons suggest that random intercept of Event significantly improves in the maximum
19
20
     model.
```

```
1
        ## ----GAMM: Accent Model---
    641
2
    642 mod2 <- bam(target ~ experience chinese +
3
    643
                     s(time elapsed, by=verb type coded) +
4
    644
                     s(log SUBTLWF Obj)+
5
    645
                     s(time elapsed, Participant.Private.ID, bs="fs", m=1)+
6
                     s(time elapsed, subject img coded, bs="fs", m=1)+
    646
7
    647
                     s(Event, bs="re"),family="binomial",
8
    648
                     data=gamm data accented, discrete=TRUE, method=" fREML")
9
    649
        summary(mod2)
```

### 10 *4.3 Results*

We observed nearly identical time course of predictive processing (Figure 11) in which restricted sentences resulted in earlier looks to the target object than nonrestrictive sentences. Further, this effect is partially reduced in accented speech in a similar manner to Porretta et al. (2020). For ggplot() code and data wrangling for visualizations, see AOW\_r\_work\_flow.rmd.

16



Figure 11. Looks to native speaker stimuli are shown in blue and non-native are shown in
yellow. Dotted lines represent restricting items, while solid lines represent non-restricting

items. The left y-axis quantifies values from our data, while the right y-axis quantifies data
 from Porretta et al. (2020).

3

### 4 *4.3.1 GLMM Results*

Results from the Main GLMM revealed a significant effect of verb\_type (β = 0.281,
SE = 0.067, z = 4.191, p < .001), indicating more looks to targets for restrictive verb\_type</li>
over non-restrictive verb\_type (Figure 12, left). Additionally, an interaction between speaker
and verb type was found (β = -0.136, SE = 0.053, z = -2.554, p = 0.011), indicating less looks
when listening to the accented speaker for restricted items. Results from the Accent GLMM
failed to reject the null hypothesis at an alpha-level of .05 (Figure 12, right).





**1** Figure 13. Model output for parsimonious GAMM models.

-	
- 1	

3

### 5. Discussion

4 5.1 Web-based Eye-Tracking May Provide Access to Unique Populations

5 Our replication results indicate that web-based eye-tracking can capture the same 6 predictive processing as in-person eye-tracking (e.g., Prystauka et al., 2023; Vos et al., 2022). 7 Our main models show that predictive sentence processing is modulated by restrictive and 8 non-restrictive verb type in line with Porretta et al. (2020) and that accented speech impedes 9 predictive processing but does not preclude it. Interestingly, our accent models did not find evidence of accent-experience modulating predictive processing. Why might this be? Our 10 wider (non-university recruited) sample of participants had far less experience with Chinese 11 accents (range = 0-3.43, M = 0.99) as compared to the students reported in Porretta et al. 12 (2020) (range = 0-3.43, M = 1.78). It is possible that the students tested in Porretta et al. 13 14 (2020) were exposed to greater Chinese-accented speech more as a result of being on a 15 university campus with international students, while our crowdsourced Prolific participants had far less exposure to Chinese-accented speech in their daily lives. If this difference in 16 17 experience with Chinese-accented English was behind the lack of evidence for an effect, this may suggest that the population available to test online is different from the population 18 19 available to test at a traditional WEIRD university setting (Rodd, in press). This speaks to the 20 potential to recruit and test far more varied bi-/multilingual populations, and potentially 21 advance theory and research on individual differences in exciting, new ways. 22 The null effect may also be due to our low statistical power. With only 49 participants

doing 24 trials, we had fewer observations per condition than is recommended (e.g., ~1,600
per condition: Brysbaert & Stevens, 2018). See our 'main power-analysis simulation' and
'accent power-analysis simulation' R scripts on OSF for post-hoc power analyses to guide
replications and extensions. Insights from the 'main power-analysis simulation' indicate that at

least 25 to 30 items per condition, with corresponding participant counts of 45 to 50, is
 necessary to achieve 80% power. For accent models, the participant number must be closer to
 90. These simulations underscore the importance of adequate sample sizes for detecting true
 effects and avoiding Type-II errors.

Finally, measurement error may have contributed to the null effect. The sliding scale used to report Chinese experience was set to start at 0 (Gorilla pre-set setting, which can be controlled in configuration settings). It could be that some of the 13 participants reporting '0' simply selected next to move on quickly. Future studies should clearly state the exact type of method used for capturing such data and make materials fully available to avoid this confusion for metrics that are essential for analyses. Our results are, therefore, inconclusive with respect to the accent models.

12

13 5.2 Best Practices for Web-Based Visual World Paradigm Eye-Tracking Research

Alone, eye-fixations are meaningless. Deriving meaning from x- and y-coordinates is achieved through time, visual stimuli, and audio stimuli. These *core four* constructs correspond directly with the variables of our experiment, research questions, and data analyses. However, managing these constructs is complex. Data wrangling through lines of code knits these constructs together, gradually constructing bridges of understanding. In what follows, we summarize best practices that are essential for bi-/multilingual reproducible webbased eye-tracking studies.

Set clear exclusion criteria for participants prior to data collection. Removal of participants given language background information or demographics should be made prior to data collection, and should involve a simple filtering step at the beginning of data wrangling. We encourage pre-registration, if possible.

Include and report behavioral/attention task checks. The decisions and standards
of participant and item removal should always be done before data analysis begins. We

recommend removal by calculating distribution-based removal standards with median
 absolute deviation (Leys et al., 2013) or standard deviation with a distribution value set
 prior to beginning wrangling. Crucially, report what criterion you used for removal (e.g., 3
 SD).

5 **Report accuracy cutoffs for participant background information.** As noted, we 6 removed one participant for reporting a different age outside our preset filter and two for 7 reporting non-monolingual status, again not in line with our preset filter. It is our 8 experience that some Prolific users may have registered their account with inaccurate 9 information in order to qualify for more studies. Ideally, researchers could pre-register 10 cutoffs and exclusion criteria.

Include and report eye-calibration. Prior to obtaining our 60 participants, 23 potential participants failed our five-point eye-calibration. In other words, roughly 20% of possible participants were unable to participate. We echo recent suggestions requiring participants to pass a specific threshold during eye-tracking calibration. Our standard of 4 out of 5 was sufficient for ensuring high quality data.

16 **Require a minimum median frame-rate greater than 5Hz.** In our study, below 5Hz is 'unusable'. Whereas the research question and effect of interest will dictate the required 17 frame-rate—consider a sentence processing study like ours which captured the native-talker 18 19 predictive effects within 6-10Hz, versus a word recognition study involving subtle voiceonset time differences which may require 20Hz to detect differences-we echo Vos et al.'s 20 21 (2022) recommendation to remove participants below the 5Hz range. However, we recommend using median frame-rate or over mean to avoid removal based on extreme trial 22 values. Removal should be reported, as well as the ranges of frame-rates. In cases of more 23 24 extensive removal, analyses should be run with both the removed participants and the full data 25 to justify removing more data.

Additionally, in an exploratory attempt, we observed that device OS and age of the
browser potentially explains variability between participants with newer device OS and more

updated browsers having better frame-rates. Additionally, Chromebooks generally provide the
 lowest frame-rates in our data. Cutoffs for types of browsers could be useful in collecting
 higher quality data and reducing the need to remove large amounts of participants found in
 other web-based eye-tracking studies (Prystauka et al., 2023).

5 Identify a quadrant classification method. Previous web-based eye-tracking studies 6 have shown that removal to the boundary of visual stimuli still enables the researcher to 7 capture results even with strict standards for removal of eye-fixations (28% in Vos et al. 8 (2022)). That is, eye-fixations outside the target areas in Figure 8 are excluded regardless 9 of how close they are to the area (i.e., classifying web-based eye-fixation the same way 10 that lab-based eye tracking does). However, ranges of removal at this strict standard 11 suggest removal of up to 93.61% of the data.

Our suggestion is twofold: firstly, embrace the noise. If unmeaningful eye-fixations are random or equally distributed from the center, then including them will not hinder analysis. Secondly, report and explore standards for maximizing signal and minimizing noise retention of eye-fixations. We suggest that future research maximize retained signal, rather than maximizing removed noise.

17 Report all time adjustments. Report any time adjustments including the 200ms required
18 to program a saccade (Matin et al., 1993) and any adjustment given a carrier phrase.

Use a meaningful eye-fixation bin size given the research question. There is an 19 20 intrinsic relationship between frame-rate and the amount of data per bin. Consider the 21 scenario where you are using a bin size of 50 with a participant with 20Hz frame-rate (i.e., 22 one eye-fixation per 50ms on average). In this scenario, each bin would only have one eye-23 fixation per bin for that participant. Along with reporting standards for binning, we recommend that the researcher find a balance between fewer bins with more data and more 24 25 bins with less data. Vos et al. (2022) and the current study used 50ms time bins. However, 26 larger bin sizes could be useful with audio stimuli with longer duration. The crucial decision

1	comes down to understanding the time-window of interest. Excluding extreme scenarios			
2	where the bin size is approaching the size of the time-window of interest, our data suggests			
3	that varying bin size has little to no effect on outcomes.			
4				
5	6. Conclusion			
6	Web-based eye-tracking is here to stay, and with that comes a demand for mastering			
7	data-wrangling skills. The choices made during web-based eye-tracking data wrangling			
8	should be documented and transparent, with key decisions always reported. We hope that the			
9	Art of Wrangling is a first step towards a more uniform approach to web-based eye-tracking			
10	in language research.			
11				
12	Data availability statement			
13	All data and scripts are available through OSF. All data is within the data folder of the			
14	OSF stored repository. All scripts are linked through Github under files on OSF (you may need			
15	to refresh the page). The primary script for data wrangling and analysis is			
16	AOW_r_work_flow.Rmd:			
17	https://osf.io/a3e5s/?view_only=822c5f28422444768729f5342fd16848			
18				
19	<b>Competing interests declaration</b>			
20	The authors declare none.			
21	Email and Postal Addresses			
22	Adam A. Bramlett: <u>abramlet@andrew.cmu.edu</u>			
23	Seth Wiener: <u>sethw1@andrew.cmu.edu</u>			
24	Department of Languages, Cultures & Applied Linguistics			
25	341 Posner Hall, 5000 Forbes Avenue			
26	Pittsburgh, PA 15213			

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